

Electronics

Simple voltage dividers

Terry Sturtevant

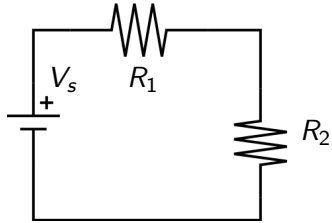
Wilfrid Laurier University

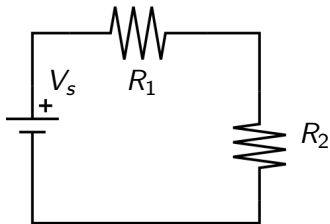
October 1, 2012

Applications of Kirchhoff's Voltage Law

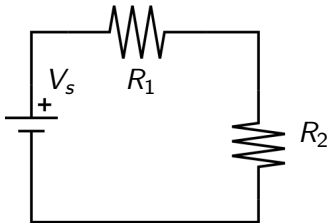
Applications of Kirchhoff's Voltage Law

Voltage dividers

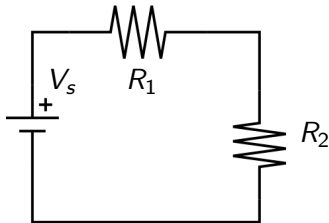




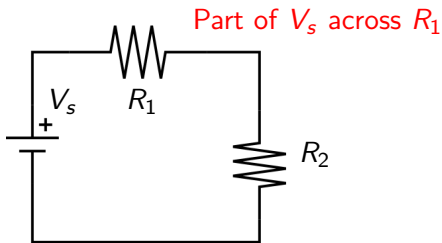
$$V_s = V_{R_1} + V_{R_2}$$



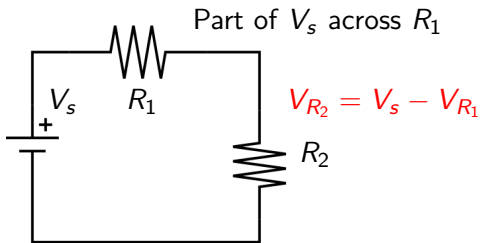
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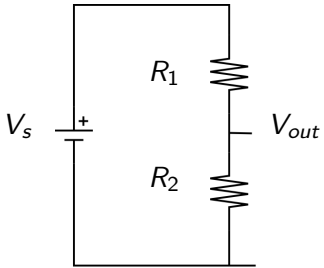
Since the current is the same in both resistors, the voltage is *divided* between the two; thus it is a **voltage divider**.

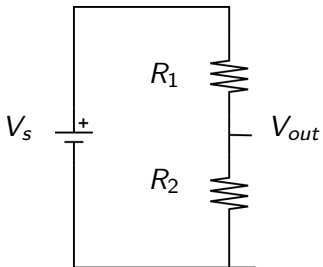
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Voltage divider circuits are very common, even when one or both circuit elements aren't resistors.

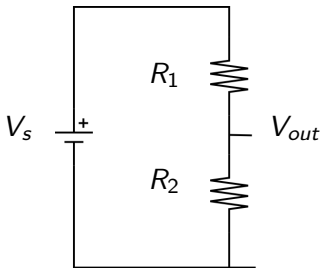
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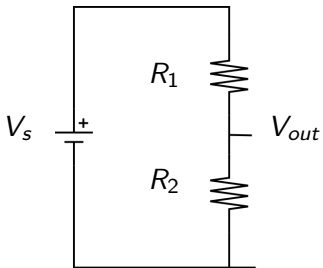


Usually a voltage divider is drawn like this so it looks like a ladder.

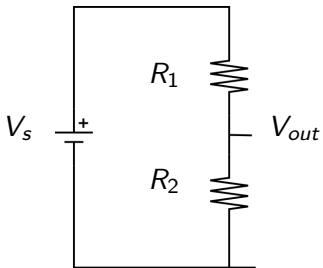


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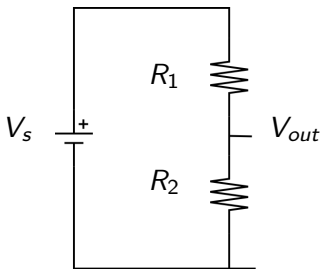
As you climb the ladder, the voltage increases.



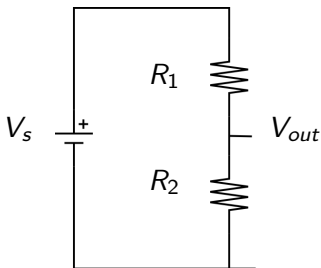
Since $I_1 = I_2$,



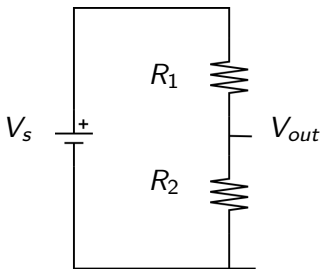
Since $I_1 = I_2$, (by Kirchhoff's current law,)



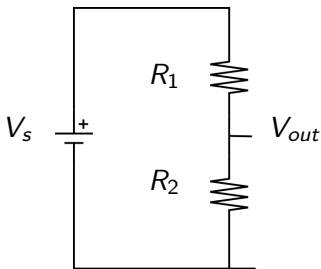
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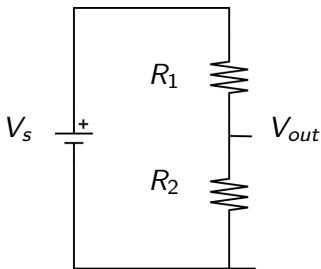
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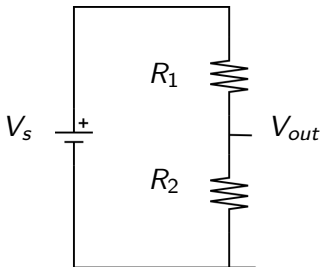


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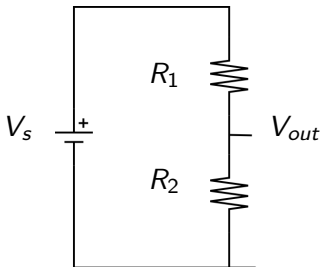


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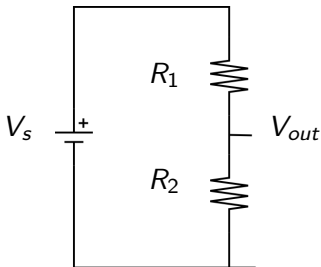
$$I = \frac{V_s}{R_1 + R_2}$$



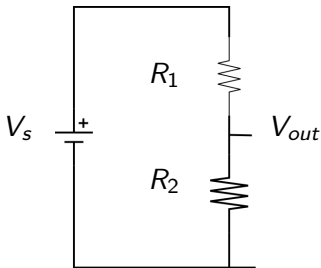
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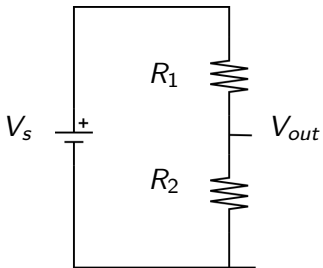
$$\begin{aligned}\text{So } V_{out} &= V_2 = IR_2 = \frac{V_s}{R_1 + R_2} R_2 \\ &= V_s \left(\frac{R_2}{R_1 + R_2} \right)\end{aligned}$$



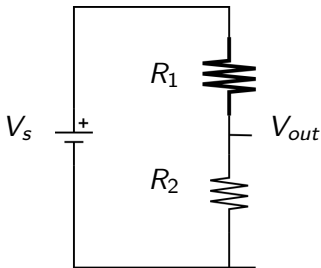
If R_1 gets *smaller*, then

$$V_{out} = V_s \left(\frac{R_2}{R_1 + R_2} \right)$$

gets *bigger*.



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If R_1 gets *bigger*, then

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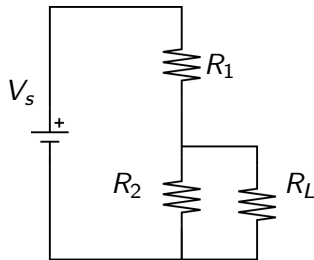
$$V_{out} = V_s \left(\frac{R_2}{R_1 + R_2} \right) = 5 \left(\frac{10}{5 + 10} \right)$$

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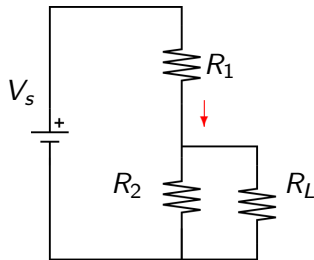
$$\begin{aligned} V_{out} &= V_s \left(\frac{R_2}{R_1 + R_2} \right) = 5 \left(\frac{10}{5 + 10} \right) \\ &= 3.3V \end{aligned}$$

Voltage divider (with load R_L)

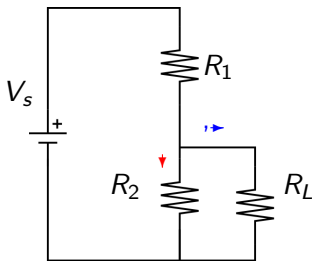


Load will reduce the output voltage

Voltage divider (with load R_L)



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Some current goes through R_2 , but some goes through R_L so the *effective* value of R_2 is reduced.

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$$\begin{aligned} \text{Parallel resistance of } R_2 \text{ and } R_L &= \frac{R_2 R_L}{R_2 + R_L} \\ &= \frac{10 \times 10}{10 + 10} = 5\Omega \end{aligned}$$

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$$= V_s \frac{R_p}{R_1 + R_p} = 5 \left(\frac{5}{5 + 5} \right)$$

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Thus V_{out}

$$= V_s \frac{R_p}{R_1 + R_p} = 5 \left(\frac{5}{5 + 5} \right)$$

$$= 2.5V$$

Variable resistors

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These are sometimes called **potentiometers** or **trimmers**.





Here is a trimmer.



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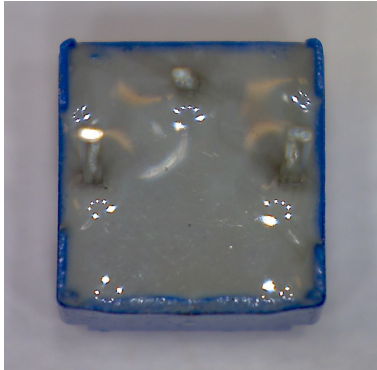
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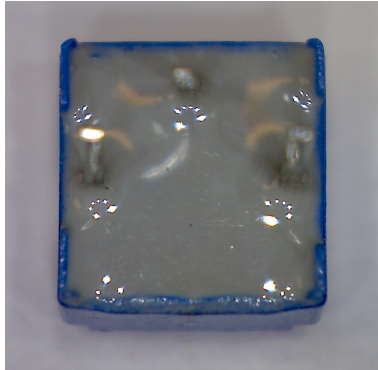
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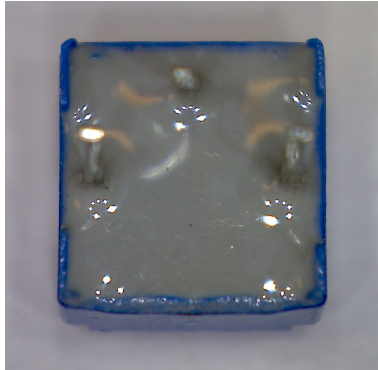
The resistance between the two end pins will be constant.

If you want a resistance which varies, just use the wiper and one end pin.

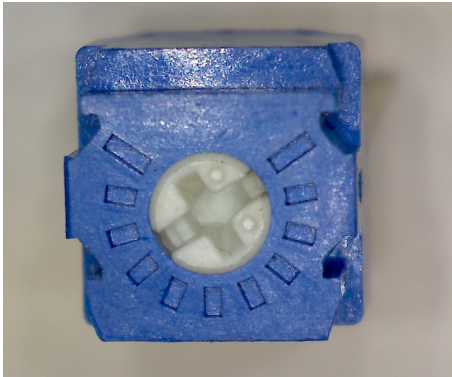


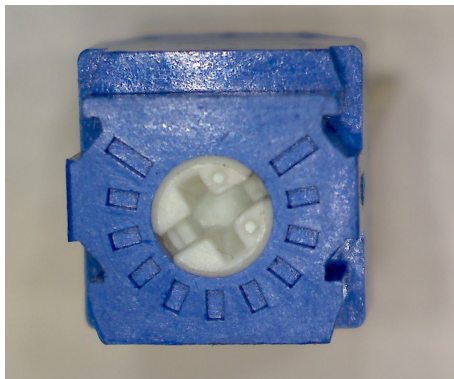


Here's a different view.

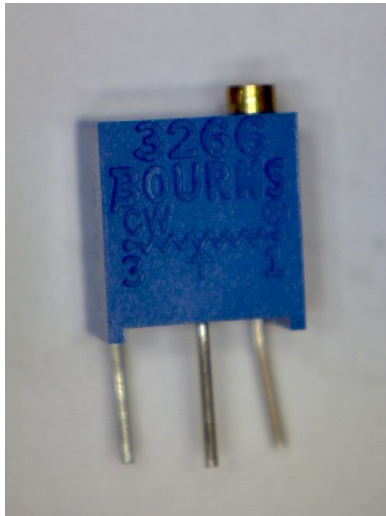


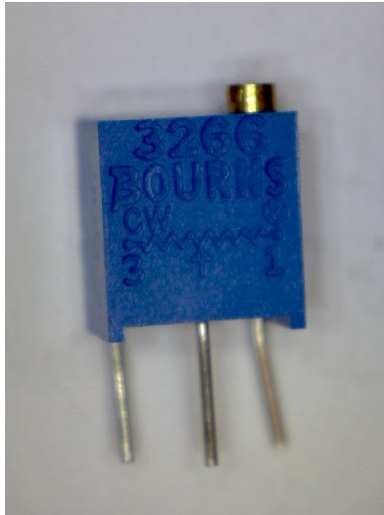
Here's a different view. The wiper is in the middle.



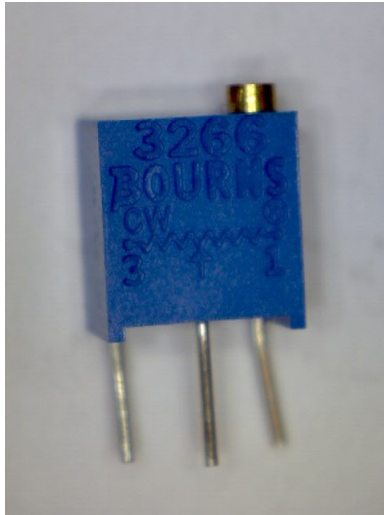


From the top, this one has 10 dashes to represent intervals of roughly $R/10$.





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Connect the two ends of your supply to the two end pins.

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Measure the output voltage on the wiper.

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